Transcriptional regulation of amino acid synthetic operons





Transcriptional Attenuation



Mechanistic sensitivity of attenuation: Hyperbolic control

The sensitivity, a_{rk}, of the regulation response, r, to the rate, k, of control codon reading, when



Mechanistic sensitivity:exponential control

m = 1, step rate for translation mk=k, average time to finish stoch. proc. 1/k *n* >> 1, step rate for transcription nq, average time to finish stoch. proc. 1/q
in the limit n → ∞

$$Q = \int_{0}^{\infty} e^{-kt} \delta(t - 1/q) dt = e^{-k/q} = r(k)$$
$$a_{rk} = \frac{d \log r}{d \log k} = -k/q = \ln(r)$$



Mechanistic sensitivity: Boolean control

m >> 1, step rate mk n >> 1, step rate nk in the limit m,k $\rightarrow \infty$ r(k) = 1 when k<q, r(k) = 0 when k>q



System sensitivity of attenuation Synthesis and consumption of limiting amino acid are equal

$$k_E[E] = f[R]v = \frac{f[R]}{\frac{1-f}{k_R} + \frac{f}{k}}$$

$$s = \frac{k_E[E]}{f[R]k_R}$$

Rate, k, of reading rare codon (f<<1) is hypersensitive ($|a_{ks}| >>1$) to amir limitation just below (s<1) balance point (s=1) of supply and demand: $a_{ks} = \frac{d \log k}{d \log s} = \frac{1}{1-s+fs}$ $f <<1 \Rightarrow a_{ks} >>1$ when $s \approx 1$

Overall sensitivity of attenuation may be numerically very large

The overall sensitivity of attenution is the mechanistic sensitivity a_{rk} multiplied by the system sensitivity a_{ks}

$$a_{rs} = \frac{d\log r}{d\log s} = \frac{d\log r}{d\log k} \cdot \frac{d\log k}{d\log s} = a_{rk} \cdot a_{ks}$$



Codon usage in attenuation leaders is highly biased. Why?



The genetic code

occorre base in couon

	U	С	Α	G	
U	Phe Phe Leu Leu	Ser Ser Ser Ser	Tyr Tyr Stop Stop	Cys U Cys C Stop A Trp G	uo
С	Leu Leu Leu Leu	Pro Pro Pro Pro	His His Gln Gln	Arg U Arg C Arg A Arg G	e in code
Α	lle lle lle Met	Thr Thr Thr Thr	Asn Asn Lys Lys	Ser U Ser C Arg A Arg G	iird base
G	Val Val Val	Ala Ala Ala	Asp Asp Glu	Gly U Gly C Gly A	Ч

tRNA isoacceptor	Codonrecognition (5'-3')		
Leu1 Leu2 Leu3 Leu4	CUG CUC CUA UUG		





Codon usage in attenuation leaders

Very highly favored codons in attenuation leaders:

Leu (CUA), Thr (ACC), Val (GUC), Ile (AUU, AUC).



Theory: Selective Charging of tRNA isoacceptors



Two isoacceptors – one codon each

$$\frac{(1-\alpha)a}{(1-\beta)b} = \frac{f_A}{f_B} \Leftrightarrow \alpha = \left(1-(1-\beta)\frac{f_A}{a} / \frac{f_B}{b}\right)$$

if
$$\frac{f_A}{a} < \frac{f_B}{b}$$
 and $\beta \to 0 \Rightarrow \alpha = \left(1 - \frac{f_A}{a} / \frac{f_B}{b}\right)$



Flow coupling relations

The two types of tRNAs are either in amino acid lacking form, *i.e.* $tRNA_A$ or $tRNA_B$ or in aminoacylated form, *i.e.* T_{3A} or T_{3B}

Define
$$[tRNA_A] + [T_{3A}] = a$$
 and $[tRNA_B] + [T_{3B}] = b$
 $[tRNA_A] = (1 - \alpha) \cdot a$ $[tRNA_B] = (1 - \beta) \cdot b$
 $[T_{3A}] = \alpha \cdot a$ $[T_{3B}] = \beta \cdot b$

Flow relations:
$$\begin{aligned} j_A &= \begin{bmatrix} AA \end{bmatrix} \begin{bmatrix} E \end{bmatrix} (1-\alpha)a = f_A \begin{bmatrix} R \end{bmatrix} v_R \\ j_B &= \begin{bmatrix} AA \end{bmatrix} \begin{bmatrix} E \end{bmatrix} (1-\beta)b = f_B \begin{bmatrix} R \end{bmatrix} v_R \end{aligned}$$

So that
$$\frac{j_A}{j_B} = \frac{a(1-\alpha)}{b(1-\beta)} = \frac{f_A}{f_B} \Longrightarrow \frac{(1-\alpha)}{(1-\beta)} = \frac{f_A/a}{f_B/b}$$

Furthermore $j = j_A + j_B = [R]v_R = [R]/\tau$ where $\tau = \frac{1}{v_{\text{max}}} \left[f_A \left(1 + \frac{K_m}{a \cdot \alpha} \right) + f_B \left(1 + \frac{K_m}{b \cdot \beta} \right) \right]$

When
$$j \to 0$$
 then $\tau \to \infty$ and $\beta \to 0, \alpha \to 1 - \frac{b/f_B}{a/f_A}$



Experimental data

For *E. coli*, total concentrations of all tRNAs and translation frequencies of all codons have been estimated.

From this information the aminoacylated fraction of each member in any family of isoacceptors can be estimated for any degree of amino acid limitation



Predictions for the leucine family



COUCHS SCHENING TO STALATION

Amino Acid	Codon	Sensitivity	Codon Usag
Leucine	UUG	0.59	6.3
	UUA	3.0	6.1
	CUG	5.5	60.1
	CUC	24.8	6.2
	CUU	24.8	5.7
	CUA	26.9	2.2
		Codo	n used in tmRI
Codon used in	attenuatio	n leader	

Codon usage in *leu* genes

Genes	Codon groups	Occurrences	Expe	
leuABCD	insensitive (UUG,UUA)	28	8-2	
	intermediate (CUG)	87	73-9	



Explaining codon usage in attenuation leaders and amino acid synthesis

By selecting the codon for which the rate of translation is most sensitive to amino acid deficiency, the codon usage in attenuators for the Leu (CUA), Thr (ACC), Val (GUC), Ile (AUU, AUC) cases were rationalized.

Frequencies of codons sensitive or insensitive to amino acid limitation are under or over represented, respectively, in genes encoding amino acid synthesizing enzymes.



Selective Charging Test 1: Direct Charging measurement



Northern hybridization

Dittmar et al. EMBO reports,2005 ehrenberg@xray.bmc.uu.se

Selective Charging Test 2: Ribsomal Bypassing at Serine codons

Bypassing Construct: ATG...... **TTC** [TCC or AGC] ATC *TAG* C *TAA* $\underline{TTT} \rightarrow \rightarrow lacZ$ Control Construct: ATG......TTC TCC GTC TAC CAG TTC $\rightarrow \rightarrow lacZ$



Selective Charging Test 3: Perturbation of tRNA concentration



Sörensen, Elf, Bouakaz et al. submitted ehrenberg@xray.bmc.uu.se

New codon reading is predicted, verified and explained



The extended reading pattern is due to a cmo5U modification of the wobble position



with G. Björk, Umeå M. Sörensen, Copenhagen T. Tenson, Tartu

Summary

- Prediction of very uneven fractions of aminoacylated tRNAs in a family of isoacceptors upon limited supply of their common amino acid.
- 2. Successful predictions of codon usage among control codons in leaders of mRNAs for operons controlled by ribosome dependent attenuation
- 3. Succesful predictions of codon usage in amino acid biosynthetic genes
- 4. Theory confirmed for four isoacceptors families with Northerns and microarrays
- 5. Successful prediction of by-passing frequencies for two tRNASer isoacceptors upon inhibition of SerRS.
- 6. Prediction and verification of novel codon assignment.



On method I

Global mathematical modeling of growing bacteria based on careful biochemistry has also explained

- 1. The *E. coli* protein elongation rate and its variation with growth condition
- 2. The missense error level in *E. coli*
- 3. The sensitivity of attenuation of transcription, i.e. 1/f effect
- 4. Bi-stability in growth rate for pathogens exposed to antibiotics
- 5. Modes of action of erythromycin and josamycin
- 6. Resistance against erythromycin and josamycin by expression of mini genes for cis acting peptides
- 7. Control of initiation of chromosome replication in *E. coli*



On Method II

The above examples high-light the power of integrating biochemistry and microbiology through mathematical modeling.

This type of modeling will also create a basis for population genetics in cell physiology



People involved

Uppsala:

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Part II: Bistability and Memory in Bacterial Responses to Antibiotics



The basic idea



Bistability







General model for antibiotic uptake in growing cells

$$\frac{da}{dt} = \underbrace{c \cdot \left(a_{ex} - a_{fr}\right)}_{J_{mem}} - \underbrace{\mu \cdot a}_{J_{gr}}$$

c permeability



Bistability in intracellular antibiotic concentration









13 inflexion point (J''_g) ,'J''_{gr}<0 $J'_{\alpha}=0$ 690



$a_{fr}(a)$ and $\mu(a)$ for ribosome inhibitors (simple model)

1. Free intracellular antibiotic is in equilibrium with ribosomes $\rightarrow a_{fr}(a)$

$$a_{fr} \cdot \left(r_t - \left(a - a_{fr}\right)\right) = K_d \cdot \left(a - a_{fr}\right) : \begin{array}{l} a_{fr} \text{ free Ab conc. (depends on a)} \\ K_d \text{ dissociation constant} \\ r_t \text{ total ribosome concentration} \end{array}$$

2. Free ribosomes translate at full rate $\rightarrow m(a)$



 V_m uninhibited protein synthesis rate r_0 concentration of amino acids in proteins



Bistability in ribsome inhibitor model



The critical cell wall permeability

$$c^{*} = \frac{v_{m}}{27\rho_{0}} \frac{\left(r_{t} - K_{d}\right)^{3}}{\left(r_{t} K_{d}\right)} \approx \frac{v_{m}}{27\rho_{0}} \frac{r_{t}^{2}}{K_{d}}$$





How long time does it take to reach steady state?





Preliminary experimental results





Experiment by Liina Kosenkranius, Tartu

Collaborators

- Johan Elf & Karin Nilsson (modeling, Uppsala)
- Tanel Tenson, Liina Kosenkranius (Experiments, Tartu)
- Arvi Jõers, Martin Lovmar (Experiments, Uppsala)





Non-competitive Inhibitors

$$E + I + S \xleftarrow{k}{q} ES + I \xrightarrow{k_c} E + P$$

$$q_I \uparrow \downarrow^{k_I} \qquad q_I \uparrow \downarrow^{k_I}$$

$$EI + S \xleftarrow{k}{q} ESI$$



Non- or uncompetitive Inhibitors





Non-competitive Inhibitors













Dichotomous codon reading during amino acid starvation



Peptide chain elongation on ribosomes



The large ribosomal subunit viewed from the the small subunit interface





The large ribosomal subunit cleaved along the nascent peptide exit tunnel







Macrolides block the peptide exit tunnel



Rate constants for erythromycin and josamycin interactions with the ribosome









Systems Biology of Antibiotic Action and Resistance



Part II: Cis-acting pentapeptides conferring erythromycin resistance

Erythromycin chased by josamycin



Erythromycin dissociates with a probability close to 1 when the resistance peptide is expressed.

Lovmar, M. et al. (2006), J Biol Chem 286, 6742-6750

Resistance peptide expression increases the erythromycin dissociation rate constant

Translated Peptide	Erythromycin dissociation rate constant (s ⁻¹)		
Init. complex	0.011 ±0.001		
MR	0.017 ±0.005		
MRL	0.025 ±0.004		
MRLF	0.051 ±0.004		
MRLFV	0.068 ±0.006		
MRLFVA	0.014 ±0.001		
MRLFVAN	0.014 ±0.001		
MN	0.011 ±0.001		
MNA	0.015 ±0.001		
MNAI	0.016 ±0.001		
MNAIK	0.017 ±0.001		
MNAIK	0.015 ±0.001		



Lovmar, M. et al. (2006), J Biol Chem 286, 6742-6750

Erythromycin and peptide dissociation rate constants

	Translated Peptide	Releasing agent	Erythromycin dissociation rate constant (s ⁻¹) ^a	Peptide diss- ociation rate constant (s ⁻¹) ^a	Peptidyl-tRNA hydrolysis rate constant (s ⁻¹) ^b
	MRLFV	RF1	0.14 ±0.02	0.073 ±0.007	
	MRLFV	RF1	No Erythromycin	0 22 +0 02	
	MRLFV	RF2	0.13 ±0.01	0.074 ±0.01	0.10 ±0.01
	MRLFV	RF2	No Erythromycin	0.25 ±0.01	0.26 ±0.03
	MRLFV	Puromycin	0.067 ±0.009	Not determined ^c	0.23 ±0.02
	MRLFV	Puromycin	No Erythromycin	Not determined ^c	0.31 ±0.03
	MRLFVA	RF2	0.014 ±0.001	0.015 ±0.002	0.015 ±0.001
	MRLFVA	RF2	No Erythromycin	0.29 ±0.03	0.32 ±0.03
	MRLFVAN	RF2	0.014 ±0.001	0.006 ±0.0004	0.004 ±0.0004
	MRLFVAN	RF2	No Erythromycin	0.27 ±0.03	0.44 ±0.03
	MNAIK	RF2	0.015 ±0.001	0.26 ±0.03	0.28 ±0.02
S.	MNAIK	RF2	No Erythromycin	0.25 ±0.02	0.27 ±0.02

^aMeasured by nitro-cellulose filter binding

^bMeasured by formic acid precipitation

°Could not be determined because fMRLFV-Puromycin bind to NC-filters

Lovmar, M. et al. (2006), J Biol Chem 286, 6742-6750

A molecular model for the mechanism of peptide mediated resistance supported by structural simulations



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Part III: Modeling erythromycin action and resistance peptide action validated in vivo

Model of erythromycin and resistance peptide action tested *in vivo*





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Part IV: Josamycin action and josamycin resistance peptides

Jocamycin and erythromycin resistance peptides differ in mode of action



Josamycin resistance peptide does not eject josamycin. Peptidyl-tRNA drop-off



Rapid josamycin induced drop-off of control, but not resistance peptidyl-tRNA





Peptidyl-tRNA hydrolase over expression confers josamycin, but not erythromycin, resistance





Systems Biology of Antibiotic Action and Resistance



Part V: Modeling josamycin action and resistance *in vivo* (in progress)

Modeling in progress

- 1. Primary effect of josamycin is induction of dipeptidyl-tRNA dropoff from a small fraction of josamycin bound ribosomes
- 2. Primary effect of josamycin resistance peptides is to sequester josamycin bound 50S subunits in the cell, thereby attenuating dipeptidyl-tRNA drop-off
- 3. The model predicts that the tRNA isoacceptor (i) with the largest ratio $(f_{2i}/[tRNA_i])$ between second position codon usage on ribosomes (f_{2i}) and total intracellular concentration ([tRNA_i]) will become sequestered as dipeptidyl-tRNA and rate limiting for bacterial growth
- 4. The model predicts that over expression of the limiting tRNA will make the tRNA with the next largest such ratio rate limiting for bacterial growth, etc etc
- 5. Accordingly, peptidyl-tRNA sequestering occurs according to a mechanism similar to that at work in selective charging of tRNA isoacceptors during starvation of their common amino acid



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